

Mathematical modeling of drying the pulped coffee (*Coffea arabica* L.) at different air conditions

RESUMO

The aim of the study was to describe the drying kinetics of washed coffee (*Coffea arabica* L.) and evaluate the best mathematical model to fit the experimental drying data conducted with different air humidity (40 %, 50 %, and 60 %) and temperatures (23 °C, 40 °C, and 60 °C). The fruit shakes were standardized washing, separation, and manual selection of green coffees, pass cane, and green buoy. Then, approx. 150 L of coffee cherries were pulped and taken directly to the yard. Drying the washed coffee was completed in a mechanical dryer and yard. The obtained results showed that the different conditions of the ambient air significantly influenced the processes of drying pulped coffee. The water content of the hygroscopic equilibrium of pulped coffee is directly proportional to the water activity and relative humidity, decreasing with increasing temperature, for the same value of equilibrium relative humidity. The Oswin model was best represented by the hygroscopicity of the pulped coffee, while the Midilli model shows the best fit to describe the drying curves of the washed coffee. The effective diffusion coefficient increases with increasing temperature of the drying air and reducing of relative humidity, being described by the Arrhenius equation

PALAVRAS-CHAVE: Drying. Mathematical Modeling. Pulped Coffee.

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INTRODUCTION

There are several factors that influence the final quality of the coffee, as soil and climate characteristics, cultivars, driving and crop management, harvesting, processing, drying, and storage. There are various forms of processing that result in major differences in the sensory attributes and there are common reports of superiority to coffee peeled and pulped and in relation to natural coffee. Drying is one of the most important stages in the processing of coffee, both from the standpoint of energy consumption and the influence this has on the operation quality of the final product. Given these problems, we seek greater control of the drying parameters (temperature of the drying air temperature of the grain mass, relative humidity, and air flow) in order to minimize adverse situations to the product. On the other hand, if the best drying techniques are not used, the quality may be impaired as a result of physical, chemical, and sensory (BORÉM et al., 2008; SAATH et al., 2010). The drying of agricultural products, thin layer, has the purpose of determining the rates of drying of the product using for data collection recording the mass loss occurred in a sample during water removal (RESENDE et al., 2009).

Thus, the drying curves, thin layer, vary with species, variety, environmental conditions, methods staging post-harvest, among other factors. Accordingly, various mathematical models have been used to describe the drying of agricultural produce, although in most cases, the semi-empirical relationships and empirical have been shown to predict the best options for the drying of grains and seeds, although its validity is restricted to the conditions under which the experimental data were obtained (RESENDE et al., 2009; CORADI et al., 2014). These models generally are based on variables external to the product, such as the temperature and relative humidity of the drying air. The semi-empirical equations are based on Newton's law of cooling heat transfer by convection, assuming that during the drying conditions are isothermal and that the water transfer is restricted to the surface of the product. Thus, the aim of the study was to describe the drying kinetics of washed coffee (*Coffea arabica* L.) and evaluate the best mathematical model to fit the experimental drying data conducted with different air humidity (40 %, 50 %, and 60 %) and temperatures (23 °C, 40 °C, and 60 °C).

MATERIAL AND METHODS

This work was conducted at the Department of Engineering and Technology Center of Post-Harvest Coffee, Federal University of Lavras. The coffee was harvested manually and selectively removing only the cherry fruit from the plant. For each repetition, 800 liters of the coffee variety Topazio were collected. All the raw materials were standardized by the washing, separation, and manual selection of green coffees; green cane passes, and buoy (Figure 1).

Figure 1 - Process of coffee stripping (left) and process of coffee pulping (right)



Fonte: Authors elaboration (2014)

Then, about 150 liters of coffee cherries were pulped and taken directly to the yard. The pulped coffee was divided into distinct segments in the yard, remaining for two days, so that the beans were taken for mechanical drying (40 and 60 ± 2 °C to 40 , 50 , and 60 ± 5 % RH) and complete drying in the yard (23 ± 2 °C to 40 , 50 , and 60 ± 5 % RH) (Figure 2).

During the time that the coffee remained in the yard, turnings were made every half hour and monitoring the temperature and relative humidity of the ambient air using a term hygrograph. Mechanical drying was conducted on two prototypes of fixed layer.

Figure 2 - Drying of natural and washed coffees in yard (left) and fixed bed dryers prototypes (right)



Fonte: Authors elaboration (2014)

To obtain the air flow diaphragm used a graduated opening in the fan inlet. The determination of the water content was performed by standard oven at 105 ± 3 °C for 24 hours (BRASIL, 2009). The drying curves were fitted to the experimental data using thirteen different semi-empirical and empirical equations discriminated below.

Equation	Models	Number
$RU = \exp(-k \cdot t)$	Newton	(1)
$RU = \exp(-k \cdot t^n)$	Page	(2)
$RU = \exp(-k \cdot t^n)$	Page Modified	(3)
$RU = \exp(-a - (a^2 + 4 \cdot b \cdot t)^{1/2}) / 2 \cdot b$	Thompson	(4)
$RU = \frac{U-U_e}{U_i-U_e} = \frac{8}{\pi} \sum_{n=0}^{\infty} \frac{1}{(2n+1)} \exp[-(2n+1)\pi D \frac{t}{4L}]$	Eight Diffusion Terms	(5)
$RU = a \cdot \exp(-k \cdot t)$	Henderson and Pabis	(6)
$RU = a \exp(-kt) + c$	Logarithmic	(7)
$RU = a \cdot \exp(-k_0 \cdot t) + b \cdot \exp(-k_1 \cdot t)$	Two Terms	(8)
$RU = a \cdot \exp(-k \cdot t) + (1 - a) \exp(-k \cdot a \cdot t)$	Two Exponential Terms	(9)
$RU = 1 + a t + b t^2$	Wang and Singh	(10)
$RU = a \cdot \exp(-k \cdot t) + b \cdot \exp(-k_0 \cdot t) + c \cdot \exp(-k_1 \cdot t)$	Henderson and Pabis Modified	(11)
$RU = a \cdot \exp(-k \cdot t^n) + b \cdot t$	Midilli	(12)
$RU = a \cdot \exp(-k \cdot t) + (1 - a) \cdot \exp(-k \cdot b \cdot t)$	Diffusion approximation	(13)

Fonte: Authors elaboration (2014)

$$RU = \frac{U^* - U_e^*}{U_i^* - U_e^*} \quad (14)$$

wherein,

U^* : water content of product (% d.b.); U_i^* : initial water content of the product (% d.b.);

U_e^* : equilibrium water content of the product (% d.b.).

It is usual to consider the value of the diffusion coefficient constant or linearly dependent on the temperature of the drying air.

$$D = A \exp\left(-\frac{E}{RT}\right) \quad (15)$$

wherein,

A: constant ($m^2 s^{-1}$); E: activation energy ($kJ kmol^{-1}$); R: universal gas constant ($8,314 kJ kmol^{-1} K^{-1}$); T_a : absolute temperature (K).

The coefficients of the Arrhenius expression were linearized by applying the logarithm of the form:

$$\ln D = \ln A - \frac{E}{RT} - \frac{1}{T_a} \quad (16)$$

To obtain the water content of the hygroscopic equilibrium of coffee the dynamic-gravimetric method was used. A desorption thin layer of the product was performed for different controlled conditions of temperature (23, 40, and 60 °C) and relative humidity of the drying air 40, 50, and 60 % until the product reached the equilibrium moisture content with air condition specified. Temperature and relative humidity were monitored by means of a psychrometer installed next to trays containing the samples. During the drying, the trays with the product were weighed periodically and the hygroscopic equilibrium was reached when the mass change of the containers to remain unchanged for three consecutive weightings. The experimental data of the equilibrium water content was adjusted mathematical models are frequently used to represent the hygroscopic agricultural products, whose expressions are shown below.

Model designation	Models	Number
Sigma Copace	$U_e^* = \exp \left\{ a - (b \cdot T) + \left[c \cdot \exp(a_w) \right] \right\}$	(17)
Sabbah	$U_e^* = a \cdot \left(a_w^b / T^c \right)$	(18)
Oswin	$U_e^* = (a + b T) / \left[(1 - a_w) / a_w \right]^{1/c}$	(19)
Henderson	$U_e^* = \left[\ln(1 - a_w) / (-a \cdot T + 273,16) \right]^{1/b}$	(20)
Henderson Modificado	$U_e^* = \left\{ \ln(1 - a_w) / [-a \cdot (T + b)] \right\}^{1/c}$	(21)
Halsey Modificado	$U_e^* = \left[\exp(a - b \cdot T) / -\ln(a_w) \right]^{1/c}$	(22)
GAB	$U_e^* = (a \cdot b \cdot c \cdot a_w) / \left[(1 - c \cdot a_w) \cdot (1 - c \cdot a_w + b \cdot c \cdot a_w) \right]$	(23)
Copace	$U_e^* = \exp \left[a - (b \cdot T) + (c \cdot a_w) \right]$	(24)
Chung Pfof	$U_e^* = a - b \cdot \ln \left[-(T + c) \cdot \ln(a_w) \right]$	(25)
BET	$U_e^* = \left\{ 1 / \left[(1 - a_w) \cdot (1/a \cdot b + ((a-1)/a \cdot b)) \right] \right\}$	(26)

Fonte: Authors elaboration (2014)

wherein,

U_e^* : equilibrium water content, % d.b.; a_w : water activity, decimal; T: temperature, °C; a, b, c: coefficients that depend on the product.

The experimental design was a completely randomized design (CRD) with three tests for each drying air velocity and drying temperatures. To adjust the mathematical models analysis were performed nonlinear regression, Quasi-Newton method, using the computer program Statistica 7.0®. To check the degree of fit of each model was considered the significance of the regression coefficient by t-test, adopting the 5% level of probability, the magnitude of the coefficient of determination (R^2), the mean relative error values (P) and the average estimated error (SE) and verified the behavior of distribution of residuals. The relative average error and the average error estimated for each model were calculated according to the following expressions, respectively:

$$P = \frac{100}{n} \sum \frac{|Y - \hat{Y}|}{Y} \quad (27)$$

$$SE = \sqrt{\frac{\sum (Y - \hat{Y})^2}{GLR}} \quad (28)$$

wherein,

Y: experimentally observed value; \hat{Y} : value calculated by the model; n : number of experimental observations; DF: degrees of freedom of the model (the number of observations minus the number of model parameters).

RESULTS AND DISCUSSION

It can be seen in Table 1 that the mathematical models used to describe the fermented coffee hygroscopicity presented, for most of its coefficients, a regression significance level of 5% probability level by the t test and, in general, the models showed values of high coefficient of determination greater than 0.90 except for the models BET, GAB, Henderson, Modified Henderson, Chung, and Pfoest that were below 80%. For further analysis, we used other statistical parameters to support the selection of the best model. Table 1 shows the summary of the mathematical models evaluated, with the parameters adjusted by nonlinear regression to the experimental data of the equilibrium moisture content of the washed coffee, obtained by desorption with the coefficients adjusted determination (R^2) and average errors for (P) and estimated (SE). It is observed in Table 1 that the equations based on the models of Oswin, Sigma Copace, and Copace showed satisfactory adjustments to the experimental data of the equilibrium moisture content of the washed coffee, with better results for the Oswin model, since it had coefficients of determination set high and average relative errors and estimated very low, independent of the temperature and relative humidity of the drying air. Therefore, when comparing the values of the equilibrium moisture content of hygroscopic coffee that was not pulped, note that the values of equilibrium water content were higher for lower temperatures and higher relative humidity of the air.

Table 1 - Parameter values estimated, mean relative error (P), standard deviation of the estimate (SE), coefficient of determination (R^2) and residual distribution for mathematical models of drying relative humidity average of 40, 50 and 60% of washed coffee (*Coffea arabica* L.)

Mathematical models	Estimation of parameters*	R^2 (%)	P (%)	SE (decimal)	Distribution of residue
			RH=40%		
Sigma copace	a = -0.642501	99.45	0.35517	0.0017	A
	b = 0.007091				
	c = -1.00785				
Sabbah	a = 0.243954	97.18	0.78707	0.0039	A
	b = 0.080254				
	c = 0.261574				

Table 1 - Parameter values estimated, mean relative error (P), standard deviation of the estimate (SE), coefficient of determination (R²) and residual distribution for mathematical models of drying relative humidity average of 40, 50 and 60% of washed coffee (*Coffea arabica* L.)-c cont.

Mathematical models	Estimation of parameters*	R ² (%)	P (%)	SE (decimal)	Distribution of residue
			RH=40%		
Oswin	a = 0.010870	99.77	0.22752	0.0011	A
	b = -0.000060				
	c = 0.063846				
Henderson	a = 0.348912	57.81	0.91484	0.0048	T
	b = 0.012984				
Henderson Modified	a = 5.860900	98.99	0.48011	0.0023	A
	b = 102.1729				
Halsey Modified	c = 0.012553	86.12	0.75809	0.0035	A
	a = -0.005891				
	b = 1.358511				
GAB	c = -2.64225	65.78	3.09819	0.0164	T
	a = 0.518185				
	b = 0.508084				
Copace	c = 0.571646	99.45	0.35509	0.0017	A
	a = -1.87077				
	b = 0.007091				
Chung Pfofost	c = -0.688173	66.83	1.01079	0.0047	T
	a = 0.02345				
	b = 0.34910				
BET	c = 0.01925	68.37	3.09819	0.0164	T
	a = 0.099957				
Corrêa	b = 18.95246	97.18	0.78700	0.0039	T
	a = 4.404755				
	b = 0.261799				
	c = 5.118700				
RH=50%					
Sigma copace	a = -0.579038	99.97	0.08480	0.0004	A
	b = 0.007495				
	c = -1.01976				
Sabbah	a = 0.225061	98.77	0.54597	0.0024	A
	b = 0.086620				
Oswin	c = 0.279099	99.99	0.05610	0.0002	A
	a = 0.008205				
	b = -0.000047				
Henderson	c = 0.081418	60.34	0.86462	0.0035	T
	a = -0.67298				
Henderson Modified	b = 0.082145	99.80	0.23084	0.0010	A
	a = 10.45824				
Halsey Modified	b = 93.12367	88.23	0.71955	0.0030	A
	c = 0.006479				
	a = -30.7154				
	b = 0.437228				
	c = -0.007432				

Table 1 - Parameter values estimated, mean relative error (P), standard deviation of the estimate (SE), coefficient of determination (R²) and residual distribution for mathematical models of drying relative humidity average of 40, 50 and 60% of washed coffee (*Coffea arabica L.*)-c cont.

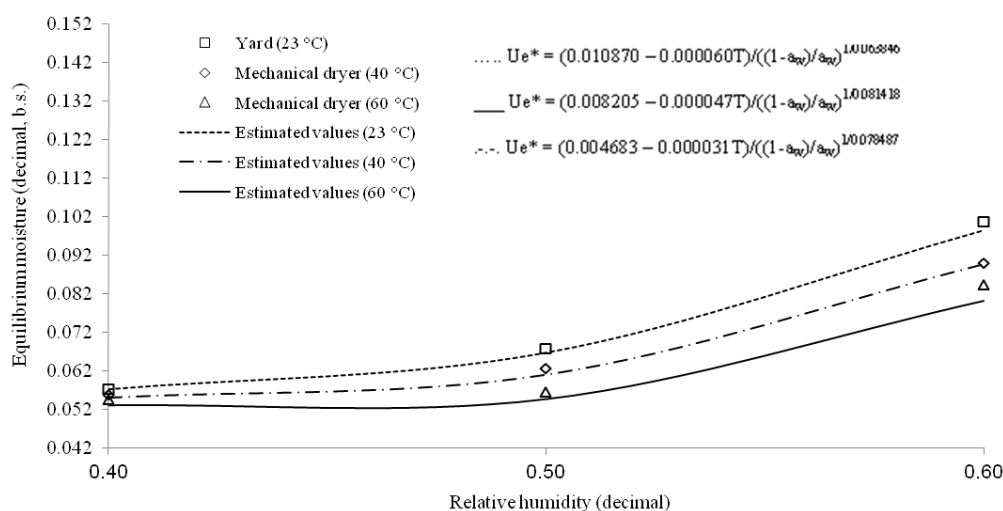
Mathematical models	Estimation of parameters*	R ² (%)	P (%)		SE (decimal)	Distribution of residue
			RH=50%			
GAB	a = 0.452697 b = 0.447961 c = 0.494803	85.12	3.11689		0.0151	T
Copace	a = -1.82833 b = 0.007495 c = -0.864013	99.97	0.08483		0.0004	A
Chung Pfof	a = 0.065384 b = -0.23489 c = 0.341839	64.91	0.43173		0.0017	T
BET	a = 0.100045 b = 25.90399	67.29	3.11689		0.0151	T
Corrêa	a = 4.707968 b = 0.279407 c = 6.202011	98.77	0.54586		0.0024	A
RH=60%						
Sigma Copace	a = -0.511717 b = 0.009224 c = -1.01499	99.87	0.21767		0.0008	A
Sabbah	a = 0.237165 b = 0.085298 c = 0.345157	99.66	0.35028		0.0013	A
Oswin	a = .004683 b = -0.000031 c = 0.078487	99.99	0.00309		0.0008	A
Henderson	a = -0.28945 b = 0.435612	62.45	0.51089		0.0017	T
Henderson Modified	a = 1.194248 b = 68.75019 c = 0.109214	99.99	0.00720		0.0000261	A
Halsey Modified	a = -35.2389 b = 0.283401 c = -0.007166	67.84	0.68119		0.0024	T
GAB	a = 0.396879 b = 0.394938 c = 0.432867	53.12	3.85968		0.0156	T
Copace	a = -1.75386 b = 0.009224 c = -1.01216	99.87	0.21771		0.0008	A
Oswin	a = -0.83451 b = 0.341892 c = 0.451280	57.26	0.85149		0.0030	T
Chung Pfof	a = 0.008205 b = -0.000047 c = 0.081418	99.99	0.05610		0.0002	A
BET	a = 0.100031 b = 38.31723	68.29	3.85968		0.0156	T
Corrêa	a = 4.377243 b = 0.346115 c = 6.261876	99.66	0.34983		0.0013	A

*All estimated coefficients were significant at 5% probability by t test. A – aleatory distribution

Fonte: Authors elaboration (2014)

The equations based on the models of Oswin, Sigma Copace, and Copace showed satisfactory adjustments to the experimental data of equilibrium moisture content of the washed coffee, with better results for the Oswin model (Table 1), since it had coefficients of determination set high and average relative errors and estimated very low, independent of temperature and relative humidity of the drying air. Therefore, when comparing the values of equilibrium moisture content of hygroscopic coffee that was not pulped, note that the values of equilibrium water content were higher for lower temperatures and higher relative humidity of the air. Figure 3 shows the experimental values of equilibrium water content of the fermented coffee obtained by desorption isotherms as well as estimated by the model Oswin. The constant water activity values of equilibrium water content of hygroscopic fermented coffee decreased with increasing temperature and with decreasing relative humidity.

Figure 3 - Observed and predicted values by Oswin model of water content equilibrium moisture content of the natural coffee obtained by desorption for different conditions of temperature and water activity. *Significant at 5% probability by the t test

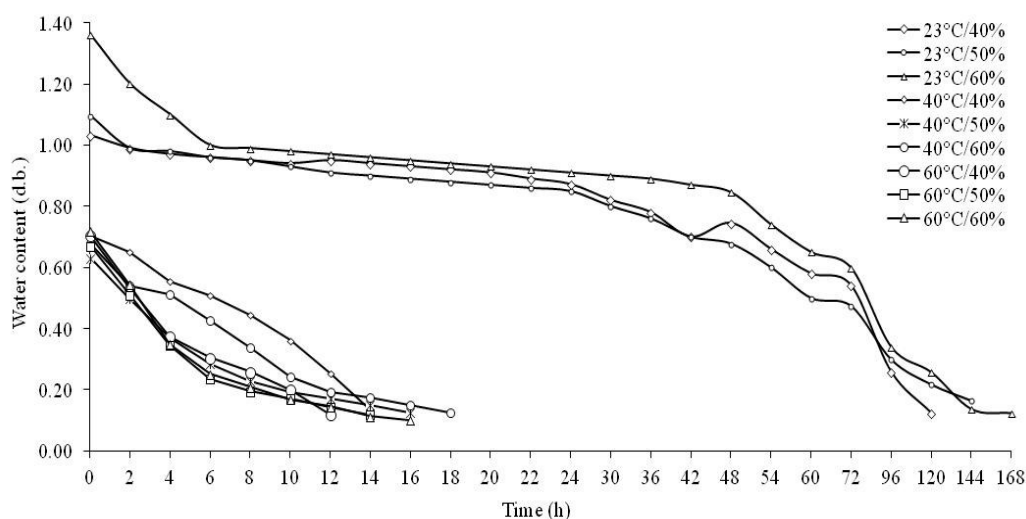


Fonte: Authors elaboration (2014)

The isotherms calculated by the pulped coffee Oswin model can be classified as type III as verified for the seeds of radish by SOUSA et al. (2013) and for crambe (SOUZA et al., 2011). Nevertheless, for most agricultural products, isotherms showed a typical sigmoidal shape (type II). Figure 4 shows the mean values of the water content of the fermented coffee beans during drying in different conditions of temperature and relative humidity. Looking at Figure 4, it is found that the time required to reach the fermented coffee water content 0.11 (d.b. decimal) was 12 to 168 h, demonstrating the

increased speed of withdrawal of water at 60°C and 40% relative humidity. As expected, the drying time is affected by air temperature, noting a greater difference between temperatures of 60 °C and 23 °C. It is also observed in Figure 4 that with increasing temperature of the drying air, there is a higher rate of removal of product water, as noted by many researchers for many agricultural products (PENA et al., 2010; REIS et al., 2011).

Figure 4 - Curves of drying coffee cherries processed naturally



Fonte: Authors elaboration (2014)

Table 2 shows the coefficients of the models adjusted for the coffee that was not pulped and that was analyzed during drying at different drying air temperatures and relative humidity conditions of the air. Among the models that gave good results, the Midilli model was selected to represent the phenomenon of drying coffee due to its simplicity compared to other models and selected to present a number of significant coefficients. It was observed that the magnitude of the drying constant (k) for the model Midilli, which represents the effect of external conditions drying increases linearly with the rise in temperature of the drying air (Table 2). The coefficient of determination was above 98% (Table 3), which according to MADAMBA et al. (1996), indicates a satisfactory representation of the phenomenon under study. According to this researcher, the use of the coefficient of determination as the only evaluation criterion for the selection of nonlinear models is not a good parameter to represent the drying phenomena.

However, analyzing the estimated average error (SE), which describes the value of the standard deviation of the estimate, it was found that the models Wang and Singh, Page, and Logarithmic Approximation of Diffusion, Midilli, Exponential for Two terms showed lower values for drying performed in different temperatures and relative humidity of the air. It is noteworthy that the lower the value of the standard deviation of the estimate (SE) is the better the quality of fit of the model will be relative to the observed data. RESENDE et al. (2009) also observed that the models Page, Diffusion Approximation and Midilli showed a low average error estimated during the modeling of drying coffee clones of *Coffea canephora*. It appears that most of the models presented values mean relative error less than 10%, which according to MOHAPATRA and RAO (2005) indicates an adequate representation of the phenomenon, except for models Thompson, Newton, Henderson, and two terms and Pabis.

Table 2. Parameters obtained from models fitted to the data for drying of washed coffee processing in the different temperatures of air drying and relative humidity of 40, 50 and 60%

Mathematical models	RH = 40%				
Exponential	T (°C)	k			
	23	0.00700			
	40	0.09313			
	60	0.33476			
Page	T (°C)	k	n		
	23	0.00045	1.55860		
	40	0.02064	1.64519		
	60	0.36838	1.00382		
Page Modified	T (°C)	k	n		
	23	0.00004	0.08424		
	40	0.09456	1.64525		
	60	0.33624	0.97149		
Thompson	T (°C)	a	b		
	23	-0.11199	1.79935		
	40	-1.00000	1.17550		
	60	-1.00000	1.08326		
Henderson and Pabis	T (°C)	a	k		
	23	1.0506	0.00751		
	40	1.0904	0.10252		
	60	0.9965	0.33358		
Logarithmic	T (°C)	a	k	c	
	23	0.42372	0.01462	0.34567	
	40	3.00380	0.02194	-1.97945	
	60	0.98510	0.34738	0.01543	
Two terms	T (°C)	a	K ₀	b	k ₁
	23	0.52538	0.00751	0.52538	0.00751
	40	0.10752	0.10252	0.54520	0.10252
	60	0.49829	0.33358	0.49829	0.33358
Two exponential terms	T (°C)	a	k		
	23	0.00486	1.41255		
	40	0.00707	12.8223		
	60	0.61493	0.40721		

Table 2. Parameters obtained from models fitted to the data for drying of washed coffee processing in the different temperatures of air drying and relative humidity of 40, 50 and 60%

Mathematical models		RH = 40%					
Wang and Sing	T (°C)	a	b				
	23	-0.00371	-0.00001				
	40	-0.06070	0.00039				
	60	-0.26310	0.01890				
Henderson and Modified Pabis	T (°C)	a	k	b	k ₀	c	k ₁
	23	0.35016	0.00749	0.35016	0.00749	0.35016	0.00751
	40	0.36346	0.10252	0.36346	0.10252	0.36346	0.10226
	60	0.33219	0.35358	0.33219	0.33358	0.33219	0.33358
Midilli	T (°C)	a	k	n	b		
	23	0.98137	-0.01081	0.63020	-0.00661		
	40	0.98716	0.02184	1.52303	-0.00597		
	60	1.00236	0.34825	0.97495	0.00042		
Diffusion approximation	T (°C)	a	k	b			
	23	-3.36765	0.01787	0.78665			
	40	-6.59768	0.22287	0.86600			
	60	0.13864	0.62679	0.49026			
Mathematical models		RH = 50%					
Exponential	T (°C)	k					
	23	0.00494					
	40	0.12325					
	60	0.37000					
Page	T (°C)	k	N				
	23	0.03218	0.60118				
	40	0.10506	1.07325				
	60	0.36838	1.00382				
Page Modified	T (°C)	k	N				
	23	0.17355	0.00004				
	40	0.12254	1.07325				
	60	0.36979	1.00383				
Thompson	T (°C)	a	b				
	23	-0.11110	1.80077				
	40	-1.00000	1.18250				
	60	-1.00000	1.08307				
Henderson and Pabis	T (°C)	a	k				
	23	0.93002	0.00422				
	40	1.00754	0.12424				
	60	1.01004	0.37375				
Logarithmic	T (°C)	a	k	c			
	23	0.52522	0.01373	0.45355			
	40	1.06942	0.10585	-0.07573			
	60	0.98503	0.41164	0.03466			
Two terms	T (°C)	a	K ₀	b	k ₁		
	23	0.148278	0.29371	0.85166	0.00338		
	40	0.503771	0.12424	0.50377	0.12424		
	60	0.505020	0.37375	0.50502	0.37375		
Two exponential terms	T (°C)	a	k				
	23	0.10511	0.03784				
	40	0.01771	6.79073				
	60	0.59498	0.46148				
Wang and Sing	T (°C)	a	b				
	23	-0.00601	0.00001				
	40	-0.09930	0.00276				
	60	-0.28540	0.02194				

Table 2. Parameters obtained from models fitted to the data for drying of washed coffee processing in the different temperatures of air drying and relative humidity of 40, 50 and 60%

Mathematical models		RH = 50%					
Henderson and Modified Pabis	T (°C)	a	k	b	k ₀	c	k ₁
	23	-0.31756	-0.00161	1.13613	0.00142	0.18148	0.09728
	40	0.33584	0.12424	0.33584	0.12424	0.33584	0.12424
Midilli	T (°C)	a	k	n	b		
	23	1.00006	0.87784	0.25203	-0.00146		
	40	0.99235	0.10855	1.02298	-0.00214		
Diffusion approximation	T (°C)	a	k	b			
	23	0.15002	0.15492	0.02165			
	40	-2.07456	0.19230	0.85655			
	T (°C)	a	k	b			
	60	0.07034	0.10727	3.80032			
		RH = 60%					
Exponential	T (°C)	k					
	23	0.00428					
	40	0.11165					
Page	T (°C)	k	n				
	23	0.09325	0.34419				
	40	0.06506	1.24176				
Page Modified	T (°C)	k	n				
	23	0.17744	0.00003				
	40	0.11070	1.18175				
Thompson	T (°C)	a	b				
	23	-0.10908	1.80400				
	40	-1.00000	1.18175				
Henderson and Pabis	T (°C)	a	K				
	23	0.88749	0.00310				
	40	1.03076	0.11535				
Logarithmic	T (°C)	a	K	c			
	23	0.395289	0.22969	0.57938			
	40	1.239563	0.07663	-0.23818			
Two terms	T (°C)	a	K ₀	b	k ₁		
	23	0.21658	-0.01740	0.95959	0.00752		
	40	0.51537	0.11535	0.51537	0.11534		
Two exponential terms	T (°C)	a	k				
	23	0.11080	0.03008				
	40	1.77245	0.15702				
Wang and Sing	T (°C)	a	b				
	23	-0.00745	0.00003				
	40	-0.08810	0.00209				
Henderson and Modified Pabis	T (°C)	a	k	b	k ₀	c	k ₁
	23	1.49017	0.00898	-0.53230	0.01601	0.00166	-0.03273
	40	0.34358	0.11534	0.34358	0.11534	0.34358	0.11534
	T (°C)	a	k	b	k ₀	c	k ₁
	60	0.33547	0.36704	0.33547	0.36704	0.33547	0.36704

Table 2. Parameters obtained from models fitted to the data for drying of washed coffee processing in the different temperatures of air drying and relative humidity of 40, 50 and 60%

Mathematical models	RH = 50%				
	T (°C)	a	k	n	b
Midilli	23	0.97188	0.00857	1.06740	0.00296
	40	0.97144	0.05386	1.31332	0.00018
	60	1.00690	0.36186	1.10794	0.00751
Diffusion approximation	T (°C)	a	k	b	
	23	0.22720	0.46930	0.00390	
	40	-4.03326	0.21346	0.86256	
	60	0.08348	0.11058	3.69000	

Fonte: Authors elaboration (2014)

The models of Thompson and Diffusion of Eight Terms achieved, for modeling the drying of washed coffee, the biased distribution of waste, thus resulting in poor fits to the experimental data, while all other models corroborated with results verified by RESENDE et al. (2009) for the modeling of drying coffee clones. All the models that were evaluated attended satisfactory the P, SE, and distribution residue, but the Midilli model was better than other evaluated because presented higher R² for all.

Table 3. Coefficients of determination (R²), mean relative errors (P) and mean estimated errors (SE) for the models analyzed during drying of the washed coffee under various temperature conditions and relative humidity of 40, 50 and 60%

Mathematical Models	UR = 40%		
	23 °C	50 °C	60 °C
	R ² (%)		
Exponential	93.86	96.45	99.81
Page	96.20	99.51	99.82
Page Modified	62.00	99.51	99.82
Thompson	55.10	55.67	48.70
Henderson and Pabis	94.25	97.19	99.81
Logarithmic	67.15	99.47	99.82
Two Terms	94.25	97.19	99.81
Two exponential terms	93.77	96.31	99.82
Wang and Singh	98.12	99.44	99.31
Henderson and Pabis Modified	94.25	97.19	99.81
Midilli	98.84	99.65	99.82
Diffusion approximation	96.36	99.23	99.82
	P (%)		
Exponential	7.13	11.74	19.57
Page	0.04	11.62	19.36
Page Modified	10.47	11.62	19.37
Thompson	60.73	79.42	32.37
Henderson and Pabis	1.56	0.88	1.47
Logarithmic	90.02	0.54	0.89
Two Terms	1.62	0.88	1.47
Two exponential terms	3.20	2.97	4.96

Table 3. Coefficients of determination (R^2), mean relative errors (P) and mean estimated errors (SE) for the models analyzed during drying of the washed coffee under various temperature conditions and relative humidity of 40, 50 and 60%

Mathematical Models	UR = 40%		
	23 °C	50 °C	60 °C
	P (%)		
Wang and Singh	7.51	8.26	13.77
Henderson and Pabis Modified	1.25	0.88	1.47
Midilli	0.03	2.55	4.24
Diffusion approximation	9.42	12.60	21.00
	SE (decimal)		
Exponential	0.0773	0.0880	0.0682
Page	0.0002	0.0347	0.0553
Page Modified	0.1837	0.0347	0.0553
Thompson	0.4777	0.5607	0.6809
Henderson and Pabis	0.0767	0.0767	0.0721
Logarithmic	0.1407	0.0352	0.0575
Two Terms	0.0848	0.0886	0.1020
Two exponential terms	0.0813	0.0951	0.0544
Wang and Singh	0.0451	0.0374	0.0720
Henderson and Pabis Modified	0.0962	0.1085	0.1442
Midilli	0.0535	0.0335	0.0727
Diffusion approximation	0.0656	0.0467	0.0618
	Distribution of residue		
Exponential	A	A	A
Page	A	A	A
Page Modified	A	A	A
Thompson	T	T	T
Henderson and Pabis	A	A	A
Logarithmic	T	A	A
Two Terms	A	A	A
Two exponential terms	A	A	A
Wang and Singh	A	A	A
Henderson and Pabis Modified	A	A	A
Midilli	A	A	A
Diffusion approximation	A	A	A
Mathematical Models	UR = 50%		
	23 °C	50 °C	60 °C
	R^2 (%)		
Exponential	91.52	99.69	99.62
Page	96.26	99.77	99.62
Page Modified	65.15	99.77	99.62
Thompson	55.68	62.81	19.38
Henderson and Pabis	93.79	99.70	99.63
Logarithmic	95.43	99.80	99.71
Two Terms	96.41	99.70	99.63
Two exponential terms	94.70	99.66	99.65
Wang and Singh	93.67	99.73	99.13
Henderson and Pabis Modified	96.46	99.70	99.63
Midilli	96.48	99.82	99.82
Diffusion approximation	96.41	99.79	99.67

Table 3. Coefficients of determination (R^2), mean relative errors (P) and mean estimated errors (SE) for the models analyzed during drying of the washed coffee under various temperature conditions and relative humidity of 40, 50 and 60%

Mathematical Models	UR = 50%		
	23 °C	50 °C	60 °C
	P (%)		
Exponential	16.23	3.66	6.11
Page	0.47	4.87	8.12
Page Modified	56.76	4.87	8.12
Thompson	25.88	58.28	63.80
Henderson and Pabis	9.38	4.12	6.87
Logarithmic	3.03	1.51	2.52
Two Terms	0.03	4.12	6.87
Two exponential terms	8.48	5.68	9.46
Wang and Singh	9.63	8.87	14.79
Henderson and Pabis Modified			
Modified	0.07	4.12	6.87
Midilli	0.01	1.95	3.25
Diffusion approximation	0.76	3.88	6.47
	SE (decimal)		
Exponential	0.0533	0.0236	0.0317
Page	0.0375	0.0218	0.0309
Page Modified	0.2225	0.0218	0.0309
Thompson	0.5054	0.4424	0.6257
Henderson and Pabis	0.0431	0.0247	0.0349
Logarithmic	0.0408	0.0202	0.0286
Two Terms	0.0406	0.0285	0.0494
Two exponential terms	0.0485	0.0265	0.0375
Wang and Singh	0.0484	0.0234	0.0331
Henderson and Pabis Modified	0.0457	0.0349	0.0699
Midilli	0.0402	0.0235	0.0406
Diffusion approximation	0.0385	0.0220	0.0337
	Distribution of residue		
Exponential	A	A	A
Page	A	A	A
Page Modified	T	A	A
Thompson	T	T	T
Henderson and Pabis	A	A	A
Logarithmic	A	A	A
Two Terms	A	A	A
Two exponential terms	A	A	A
Wang and Singh	A	A	A
Henderson and Pabis Modified	A	A	A
Midilli	A	A	A
Diffusion approximation	A	A	A
	UR = 60%		
	R^2 (%)		
Exponential	51.31	98.67	99.63
Page	65.68	99.30	99.64
Page Modified	52.10	99.30	99.64
Thompson	58.23	55.42	11.92
Henderson and Pabis	58.35	98.76	99.64
Logarithmic	65.27	99.24	99.71

Table 3. Coefficients of determination (R^2), mean relative errors (P) and mean estimated errors (SE) for the models analyzed during drying of the washed coffee under various temperature conditions and relative humidity of 40, 50 and 60%

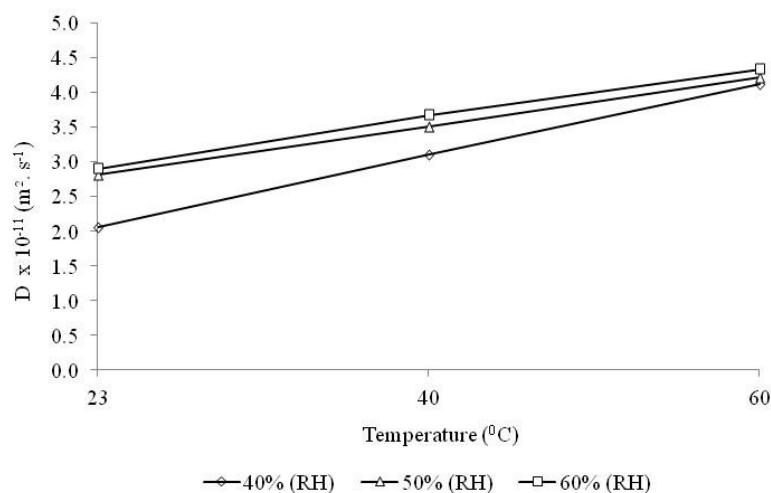
Mathematical Models	UR = 60%		
	23 °C	50 °C	60 °C
R^2 (%)			
Two Terms	70.85	98.76	99.64
Two exponential terms	57.38	99.32	99.67
Wang and Singh	69.03	99.39	99.00
Henderson and Pabis Modified	74.37	98.76	99.64
Midilli	67.08	99.45	99.77
Diffusion approximation	65.36	99.34	99.69
P (%)			
Exponential	25.40	1.65	2.75
Page	0.09	7.87	13.12
Page Modified	74.32	7.87	13.12
Thompson	30.79	73.53	89.21
Henderson and Pabis	14.63	4.57	7.62
Logarithmic	3.51	0.23	0.39
Two Terms	5.41	4.57	7.62
Two exponential terms	17.35	7.93	13.22
Wang and Singh	53.79	54.76	91.27
Henderson and Pabis Modified	6.01	4.57	7.62
Midilli	4.75	6.57	10.95
Diffusion approximation	0.14	6.56	10.93
SE (decimal)			
Exponential	0.1357	0.0509	0.0682
Page	0.1245	0.0391	0.0553
Page Modified	0.2618	0.0391	0.0553
Thompson	0.5359	0.4815	0.6809
Henderson and Pabis	0.1297	0.0510	0.0721
Logarithmic	0.1248	0.0407	0.0575
Two Terms	0.1287	0.0589	0.1020
Two exponential terms	0.1352	0.0385	0.0544
Wang and Singh	0.1195	0.0509	0.0720
Henderson and Pabis Modified	0.1375	0.0721	0.1442
Midilli	0.1350	0.0420	0.0727
Diffusion approximation	0.1310	0.0405	0.0618
Distribution of residue			
Exponential	A	A	A
Page	A	A	A
Page Modified	T	A	A
Thompson	T	T	T
Henderson and Pabis	A	A	A
Logarithmic	A	A	A
Two Terms	A	A	A
Two exponential terms	A	A	A
Wang and Singh	A	A	A
Henderson and Pabis Modified	A	A	A
Midilli	A	A	A
Diffusion approximation	A	A	A

A – aleatory distribution

Fonte: Authors elaboration (2014)

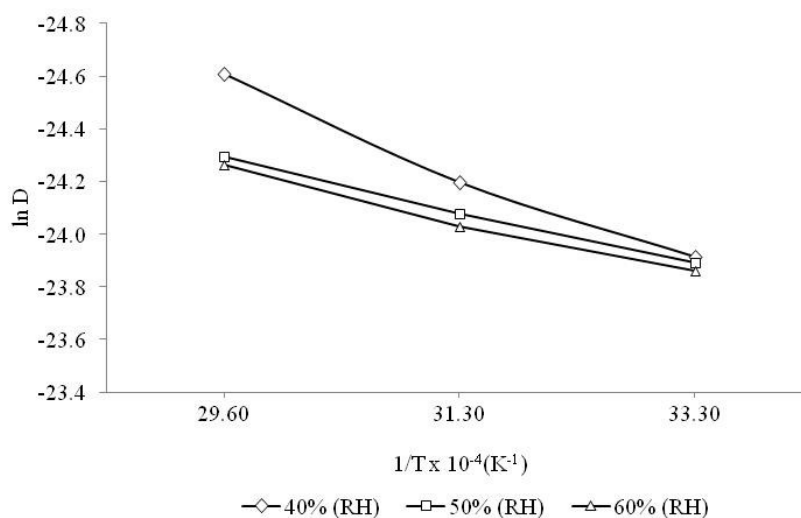
Figure 5 shows the values of the effective diffusion coefficient for the pulped coffee beans during different drying conditions. It appears that during the drying the effective diffusion coefficient increased significantly ($p < 0.05$), with the rise of temperature and increase in relative humidity. ALMEIDA et al. (2009) found that during the drying of adzuki effective diffusion coefficients had magnitudes between 0.51×10^{-10} and $2.23 \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$ for the temperature range from $30 \text{ }^\circ\text{C}$ to $70 \text{ }^\circ\text{C}$. Their dependence on the temperature of the drying air is described by the Arrhenius equation as shown in Figure 6.

Figure 5 - Values for the effective diffusion coefficient ($\text{m}^2 \text{ s}^{-1}$), due to different air temperatures drying of pulped coffee.



Fonte: Authors elaboration (2014)

Figure 6 - Representation Arrhenius relationship for the effective diffusivity and air temperature drying of natural coffee.



Fonte: Authors elaboration (2014)

The almost linear fit was obtained indicates that uniform variation of diffusivity with temperature, the value being the variation of diffusivity coefficient obtained at 60 °C, slightly higher than the temperatures of 23 °C and 40 °C, this may be explained due to the molecular vibration of water, because, according GONELI et al. (2011), the diffusion coefficient of variation effective occurs with increasing temperature, which increases the molecular vibration of water molecules and contributes to a faster diffusion. It can be said, therefore, that there was a greater diffusion at a temperature of 60°C. It is observed that the values of Ln (D) as a function of the inverse absolute temperature ($1/T_a$) show similar behavior to the ranges of temperature 23 °C to 40 °C and 40 °C to 60 °C. Therefore, it can be inferred that there was no interference of external conditions or drying temperatures.

CONCLUSIONS

The different conditions of the ambient air significantly influenced the processes of the drying pulped coffee. The water content of the hygroscopic equilibrium of pulped coffee is directly proportional to the water activity and relative humidity, decreasing with increasing temperature, for the same value of equilibrium relative humidity. The Oswin model was best represented with the hygroscopicity of the pulped coffee, while the Midilli model shows the best fit to describe the drying curves of the washed coffee. The effective diffusion coefficient increases with increasing temperature of the drying air and reducing relative humidity as described by the Arrhenius equation.

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Modelagem matemática da secagem do café despulpado em diferentes condições do ar

ABSTRACT

O objetivo do estudo foi descrever a cinética de secagem do café despulpado (*Coffea arabica* L.) e avaliar o melhor modelo matemático para ajuste dos dados experimentais de secagem, realizada com diferentes umidades relativas do ar (40, 50 e 60 %) e temperaturas (23, 40 e 60 °C). Os frutos de cafés foram padronizadas na lavagem, separação e seleção manual, dos cafés verdes, passa cana, verde e boia. Em seguida, cerca de 150L de café cereja foi despulpado e levado diretamente para o terreiro. A secagem do café despulpado foi completada em um secador mecânico e no terreiro. Os resultados obtidos mostraram que as diferentes condições do ar ambiente influenciou significativamente nos processos de secagem do café despulpado. O teor de água de equilíbrio higroscópico do café despulpado é proporcional à atividade de água e a umidade relativa, diminuindo com o aumento da temperatura, para o mesmo valor de umidade de equilíbrio higroscópico. O modelo Oswin foi o que melhor representou a higroscopicidade do café despulpado, enquanto o modelo Midilli apresentou o melhor ajuste das curvas de secagem do café. O coeficiente de difusão eficaz aumentou com o aumento da temperatura do ar de secagem e redução da umidade relativa, sendo descrito pela equação de Arrhenius.

KEYWORDS: Coffea arabica L. Secagem. Modelagem Matemática. Café Despulpado.

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